

Exam. Code : 108506

Subject Code : 501093

B.Com. 6<sup>th</sup> Semester (Batch 2022-25)

**OPERATIONS RESEARCH**

**Paper—BCG-603**

Time Allowed—3 Hours] [Maximum Marks—50

**Note** :— Attempt **FIVE** questions in all, selecting at least **ONE** question from each section. The fifth question may be attempted from any section. All questions carry equal marks.

**SECTION—A**

1. Define Operations Research. Elucidate its characteristics and limitations.
2. Solve the following problems by Simplex method :

$$\text{Max. } Z = 2x_1 + 5x_2 + 7x_3$$

Subject to

$$3x_1 + 2x_2 + 4x_3 \leq 100$$

$$x_1 + 4x_2 + 2x_3 \leq 100$$

$$x_1 + x_2 + 3x_3 \leq 100$$

$$x_1, x_2, x_3 \geq 0$$

## SECTION—B

3. Solve the following transportation problem, whose cost matrix availability at each point and requirements at each warehouse are given as follows :

| Plants              | Warehouses |       |       |       | Availability |
|---------------------|------------|-------|-------|-------|--------------|
|                     | $W_1$      | $W_2$ | $W_3$ | $W_4$ |              |
| $P_1$               | 190        | 300   | 500   | 100   | 70           |
| $P_2$               | 700        | 300   | 400   | 600   | 90           |
| $P_3$               | 400        | 100   | 600   | 00    | 180          |
| <b>Requirements</b> | 50         | 80    | 70    | 140   |              |

4. A production supervisor is considering how he should assign five jobs that are to be performed to five operators. He wants to assign the jobs to the operators in such a manner that the aggregate cost to perform the job is the

least. He has the following information about the wages paid to the operators for performing these jobs :

| Operators | Jobs |    |   |   |    |
|-----------|------|----|---|---|----|
|           | 1    | 2  | 3 | 4 | 5  |
| A         | 10   | 3  | 3 | 2 | 8  |
| B         | 9    | 7  | 8 | 2 | 7  |
| C         | 7    | 5  | 6 | 2 | 4  |
| D         | 3    | 5  | 8 | 2 | 4  |
| E         | 9    | 10 | 9 | 6 | 10 |

Assign the jobs to the operators so that the aggregate cost is the least.

### SECTION—C

5. At a service counter of fast food joint, the customers arrive at the average interval of 6 minutes whereas the counter clerk takes on an average 5 minutes for preparation of bill and delivery of the item. Calculate the following :
- (a) Utilization factor.

- (b) Average waiting time of the customers at the fast food joint.
- (c) Expected average waiting time in the line.
- (d) Average number of customers in the service counter area.
- (e) Average number of customers in the line.
- (f) Probability that the counter clerk is idle.
- (g) Probability of finding the clerk busy.
- (h) Changes that customer is required to wait more than 30 minutes in the system.
- (i) Probability of having 4 customers in the system.
- (j) Probability of finding more than 3 customers in the system.

6. Using the dominance property obtain the optimal strategies for both the players and determine the value of the game. The pay off matrix for player A is given :

|                 |                 |          |           |            |           |          |
|-----------------|-----------------|----------|-----------|------------|-----------|----------|
| <b>Player A</b> | <b>Player B</b> |          |           |            |           |          |
|                 |                 | <b>I</b> | <b>II</b> | <b>III</b> | <b>IV</b> | <b>V</b> |
|                 | <b>I</b>        | 2        | 4         | 3          | 8         | 4        |
|                 | <b>II</b>       | 5        | 6         | 3          | 7         | 8        |
|                 | <b>III</b>      | 6        | 7         | 9          | 8         | 7        |
|                 | <b>IV</b>       | 4        | 2         | 8          | 4         | 3        |

### SECTION—D

7. (a) Differentiate between PERT and CPM. Give appropriate examples.
- (b) A project is composed of 11 activities, the time estimates for which are given below :

| <b>Activity</b> | <b>A (days)</b> | <b>B (days)</b> | <b>M (days)</b> |
|-----------------|-----------------|-----------------|-----------------|
| 1-2             | 7               | 17              | 9               |
| 1-3             | 10              | 60              | 20              |
| 1-4             | 5               | 15              | 10              |
| 2-5             | 50              | 110             | 65              |
| 2-6             | 30              | 50              | 40              |

| Activity | A (days) | B (days) | M (days) |
|----------|----------|----------|----------|
| 3-6      | 50       | 90       | 55       |
| 3-7      | 1        | 9        | 5        |
| 4-7      | 40       | 68       | 48       |
| 5-8      | 5        | 15       | 10       |
| 6-8      | 20       | 52       | 27       |
| 7-8      | 30       | 50       | 40       |

(i) Draw the network diagram.

(ii) Determine the critical path.

8. Characteristics of a project schedule are given below :

| Activity   |            | Activity Time   |                  |                  |
|------------|------------|-----------------|------------------|------------------|
| Tail Event | Head Event | Optimistic Time | Pessimistic Time | Most Likely Time |
| i          | j          | ( $t_o$ )       | ( $t_p$ )        | ( $t_m$ )        |
| 1          | 2          | 1               | 3                | 2                |
| 2          | 3          | 1               | 7                | 4                |
| 2          | 7          | 2               | 4                | 3                |
| 3          | 4          | 1               | 5                | 3                |
| 3          | 5          | 0               | 0                | 0                |
| 4          | 6          | 0               | 0                | 0                |
| 5          | 6          | 3               | 13               | 5                |
| 7          | 8          | 4               | 12               | 8                |
| 6          | 9          | 4               | 14               | 6                |
| 8          | 9          | 1               | 3                | 2                |

Determine :

- (a) Expected activity times
- (b) Earliest expected and latest expected time for each event. Gndupapers.com
- (c) Draw a network and indicate the critical path on it.
- (d) Determine the scheduling of activities and compute various floats.